Modeling and simulation of an electrolyser for the production of HHO in Matlab-Simulink®

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ABSTRACT

The electrolyzers work through an electrochemical process, their derivatives (H₂, O₂, and HHO) are used as enriching fuels due to the electrolysis of water, being cleaner than gasoline and diesel. This article presents the dynamic model of an alkaline electrolyzer that uses an electrolyte (KOH or NaHCO₃) dissolved in distilled water to accelerate the production of oxyhydrogen (HHO). The model shows the phase change that occurs inside the electrolytic cell. The EES® software was used to determine the values of enthalpy, entropy, and free energy that vary during the electrochemical reaction; the equations were simulated in Matlab-Simulink® to observe their dynamic behavior. The Simulations presented varying every 5 g the electrolyte until reaching 20 g. The flow rate of HHO with potassium hydroxide (20 g) is higher than 0.02 L/s, and with sodium bicarbonate (20 g) it is above 0.0006 L/s, confirming what the literature of alkaline cells state, that the most efficient electrolyte for its energy conversion is KOH.

RESUMEN

Los electrolizadores funcionan mediante un proceso electroquímico, sus derivados (H₂, O₂, y HHO) debido a la electrólisis del agua son utilizados como combustibles enriquecedores, siendo más limpios que la gasolina y diesel. Este artículo presenta el modelo dinámico de un electrolizador alcalino que utiliza un electrolito (KOH o NaHCO₃) disuelto en agua destilada para acelerar la producción de oxihidrógeno (HHO). El modelo muestra el cambio de fase que ocurre en el interior de la celda electrolítica. Se utilizó el software EES® para determinar los valores de entalpía, entropía, y energía libre que varían durante la reacción electroquímica; las ecuaciones fueron simuladas en Matlab-Simulink® para observar su comportamiento dinámico. Las simulaciones fueron realizadas variando cada 5 g el electrolito hasta llegar a 20 g. El caudal de HHO con potasio hidroxido (20 g) es superior a 0.02 L/s, y con bicarbonato de sodio (20 g) está por encima de 0.0006 L/s, confirmando lo que se enuncia en la literatura de celdas alcalinas, donde se establece que el electrolito más eficiente para su conversión energética es KOH.

Introduction

Voltaic cells and electrolytic cells are fuel cells that operate by means of an electrochemical process in which reagents and products are subjected to an energy imbalance due to the fact that the reaction can be exothermic (it gives off energy) or endothermic (it needs to be supplied with energy), from this perspective the spontaneity of these devices is studied [1].
Fuel cells are a cleaner choice compared to gasoline and diesel used in internal combustion engines [2]. The efficiency of the cells is another parameter that must be taken into account, being approximately twice as high as the thermal engines because the latter are affected by the following limitations established by Carnot’s Theorem [3].

There are several types of fuel cells, currently the classification that is made for these devices is taking into account the type of electrolyte they use, this way we have the AFC (Alkaline Fuel Cells), PEMFC (Proton Exchange Membrane Fuel Cells), DMFC (Direct Methanol Fuel Cells), PAFC (Phosphoric Acid Fuel Cells), MCFC (Fused Carbonate Fuel Cells) and SOFC (Solid Oxide Fuel Cells) [2]. The versatility of the cells has allowed them to have a field of application in the industry specifically in transportation, stationary power systems and portable systems, the last three sectors is where its impact has been most noticeable [1], [4].

The effect caused by fuel cells in industry is largely due to their efficiency in conversion and energy input, to understand the above is necessary to understand the principle of operation of these devices being necessary to identify the mathematical equations that model their dynamic behavior.

In this article the modeling of an electrolyzer or alkaline electrolytic cell (AFC) with a single output will be carried out, for the study of the production of oxyhydrogen gas (HHO) as a clean energy, in this way it can be used as an enriching fuel or enhancer in the processes where combustion takes place. In this research, concepts of thermodynamics, chemistry, thermochemistry, and electrochemistry are taken into account for the approach of the equations, thus enunciating a thermodynamic model, electric model, chemical model, and thermal model. The EES software is used to determine the value of the variables of the thermodynamic model (enthalpy, entropy and free energy), the equations of the other models are simulated in Matlab-Simulink® because some do not present linearity, and others are empirical electrochemical relations.

The electrolysis of water in an alkaline medium in an electrolyser is generated by means of a redox reaction (oxidation - reduction) that occurs in the electrodes [5], this process is shown in Figure 1.

**Materials and methods**

**Alkaline electrolytic cell**

The phase change (liquid to gaseous state) of the water that occurs in the alkaline electrolyser to be modelled, occurs when energy is supplied to the electrochemical reaction in the form of electrical work (non-spontaneous process) [5], [6].

In order to know in detail what happens in the electrodes of the cell, the generation of gaseous oxygen in the anode is presented by means of (1), and the generation of gaseous hydrogen is shown in the cathode with (2).

**Anode:**

$$2OH^- (aq) \rightarrow \frac{1}{2} O_2 (g) + H_2O(l) + 2e^- \quad (1)$$

Where:
OH$^−$ (aq): Hydroxyl ion (water-based solution)
$O_2$(g): Oxygen (gaseous)
$H_2O(l)$: Water (Liquids)
e$^−$: Electrons

Cathode:

\[2H_2O(l) + 2e^− \rightarrow H_2(g) + 2OH^− (aq) \quad (2)\]

Where:

$H_2(g)$: Hydrogen (gaseous)

The two previous semirreactions allow to arrive at the general reaction (3) that governs the process, it is necessary to mention that the change of phase that is carried out is thanks to the electrolysis (decomposition of the water molecule by the passage of the current in it) [7].

\[H_2O(l) + W_đéctrico \rightarrow H_2(g) + \frac{1}{2}O_2(g) \quad (3)\]

**Alkaline electrolytic cell modeling**

Figure 2 shows the electrolyzer modeled in SolidWorks®, consisting of a stack of cells composed of 9 plates (1 positive, 2 negative, and 6 neutral) of 316 stainless steel, 2 sheets of acrylic, and 10 PVC rings.

In the electrolytic cell there is a conversion of electrical energy to chemistry, in this process there are some thermodynamic variables that suffer energy imbalance, it is for this reason that the mathematical model is divided into four stages: thermodynamic model, electrical model, chemical model, and thermal model.

**Thermodynamic model**

To get the most energy available for useful work, a status function, called free energy (G) [7], [8], is defined by (4).

\[ΔG = ΔH − TΔS \quad (4)\]

Where:

$ΔH$: Change of enthalpy
$ΔS$: Change of entropy
$ΔG$: Free energy exchange
$T$: Temperature

In a non-spontaneous electrochemical process the change of free energy ($ΔG$) is equivalent to the electrical work ($W_đéctrico$) that is necessary to supply for the reaction to occur [9], in (5) the above can be appreciated, non-spontaneity is represented by leaving the work expressed in a positive way.
\[ \Delta G = W_{electric} \quad (5) \]

The electrical work is equivalent to the irreversible voltage \( (U_{irrev}) \) of the electrolyser, for this reason the above equation is expressed with a voltage that is irreversible by the present losses \([10]\) by means of \((6)\).

\[ U_{irrev} = \frac{\Delta G}{zF} \quad (6) \]

Where:
\begin{align*}
  z & : \text{Number of electrons (} 2e^- \text{)} \\
  F & : \text{Faraday Constant (96500 C)}
\end{align*}

When a reversible reaction is assumed, i.e. without losses, the process energy \( (H) \) is worked with as shown in \((7)\) with a reversible voltage \( (U_{rev}) \).

\[ U_{rev} = \frac{\Delta H}{zF} \quad (7) \]

The effect of irreversibilities (losses) can be seen when calculating the irreversible and reversible voltages that result in \( U_{irrev} = 1.22 \text{ v} \) and \( U_{rev} = 1.48 \text{ v} \), these stress values were calculated from enthalpy and entropy values under standard reaction conditions, i.e. at 25 °C and 1 bar.

The electric model is designed to determine the current \( (I) \) and voltage of the electrolyzer, the relationship between these two variables is modeled by means of \((8)\) found in \([11],[12]\).

\[ U = U_{rev} + \frac{r}{A} I + s \left[ \log\left( \frac{T}{T_A} I + 1 \right) \right] \quad (8) \]

Where:
\begin{align*}
  r,s,t & : \text{Coefficients} \\
  A & : \text{Electrode area}
\end{align*}

\[ U = U_{rev} + \frac{r_i + r_s T}{A} I + s \left[ \log\left( \frac{t_i + t_s + T}{T_A} I + 1 \right) \right] \quad (9) \]

The coefficients \( r, s, t \) model the overvoltages (irreversibilities), to express their value in a more precise way they are left expressed in such a way that they depend on the temperature through \((9)\), so it is stated \([12],[13]\).

<table>
<thead>
<tr>
<th>Coefficient</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>( r_i )</td>
<td>8.058e-5</td>
<td>( \Omega m^2 )</td>
</tr>
<tr>
<td>( r_s )</td>
<td>-2.5e-7</td>
<td>( \Omega m^2 \cdot C^{-1} )</td>
</tr>
<tr>
<td>( s )</td>
<td>0.185</td>
<td>V</td>
</tr>
<tr>
<td>( t_i )</td>
<td>1.002</td>
<td>( A^{-1}m^2 )</td>
</tr>
<tr>
<td>( t_s )</td>
<td>8.424</td>
<td>( A^{-1}m^2 \cdot C )</td>
</tr>
<tr>
<td>( t_A )</td>
<td>2473</td>
<td>( A^{-1}m^2 \cdot C^2 )</td>
</tr>
</tbody>
</table>

Source: \([11]\)

The power consumed by the cell is directly proportional to the number of cells \( (N) \) that make up the stack, this relationship is established with \((10)\).

\[ W_{electric} = NIU \quad (10) \]

The calculation is made by means of the product between the number of cells connected in series \( (n_r) \) with the number of cells connected in parallel \( (n_p) \) by means of \((11)\).

\[ N = (n_r)(n_p) \quad (11) \]

By setting the temperature \( (T) \) of the electrolyte this part consists of 2 equations (power consumed with \((10)\), and voltage between electrolyser terminals expressed in \((9)\)) with 2 unknowns \( (U, I) \) and its resolution determines the operating point of the electrolyser.

**Chemical model**

Faraday’s law states that the rate of production of oxyhydrogen in a cell is proportional to the transfer of electrons in the electrodes, i.e., to the intensity supplied by the electrical work, \((12)\) shows this relationship \([11]\).

\[ v_{HHO} = n_f \frac{NI}{zF} \quad (12) \]

The expression used for the calculation of Faraday’s Efficiency is that proposed by \([11]\), where the effect of stray currents is modelled. It is determined by means of \((13)\), is caused by stray currents and these increase by current densities.
The dependence of the coefficients $f_1$ and $f_2$ with the temperature is obtained by means of the experimental tests carried out by [11], by means of measurements in different points of operation, obtaining polynomial expressions depending on the temperature with (14), and (15).

\[ f_1(T) = a_{f_1} \cdot T + b_{f_1} \]  \hspace{1cm} (14)

\[ f_2(T) = c_{f_2} \cdot T^2 + d_{f_2} \cdot T + e_{f_2} \]  \hspace{1cm} (15)

In the calculation of Faraday’s Efficiency the values of $f_1$ and $f_2$, in Table II you can see these data for certain temperatures, enunciated by [11].

<table>
<thead>
<tr>
<th>Coefficient</th>
<th>Value</th>
<th>Temperature</th>
</tr>
</thead>
<tbody>
<tr>
<td>$f_1$</td>
<td>150 mA$^2$cm$^{-4}$</td>
<td>40 °C</td>
</tr>
<tr>
<td>$f_2$</td>
<td>200 mA$^2$cm$^{-4}$</td>
<td>60 °C</td>
</tr>
<tr>
<td>$f_1$</td>
<td>250 mA$^2$cm$^{-4}$</td>
<td>80 °C</td>
</tr>
<tr>
<td>$f_1$</td>
<td>250 mA$^2$cm$^{-4}$</td>
<td>80 °C</td>
</tr>
<tr>
<td>$f_2$</td>
<td>0.990</td>
<td>40 °C</td>
</tr>
<tr>
<td>$f_2$</td>
<td>0.985</td>
<td>60 °C</td>
</tr>
<tr>
<td>$f_2$</td>
<td>0.980</td>
<td>80 °C</td>
</tr>
<tr>
<td>$f_2$</td>
<td>0.960</td>
<td>80 °C</td>
</tr>
</tbody>
</table>

Source: [11]

With the data from Table II, the coefficients of the polynomials (17) and (18) are calculated by making an adjustment of minimum squares to relate $f_1$, and $f_2$ with temperature, because the function is not known.

Figure 3 shows a straight line (grade 1 polynomial), because a linear dependence on the temperature of the electrochemical reaction has been assumed in the least squares setting.

\[ n_F = f_2 \frac{(I / A)^2}{(I / A)^2 + f_1} \]  \hspace{1cm} (13)

Of (17) we have:

\[ a_{f_1} = 2.5 \frac{mA^2}{cm^4} \]

\[ b_{f_1} = 50 \frac{mA^2}{cm^4} \]

Figure 4 shows a curve (grade 2 polynomial), because a quadratic dependence on the temperature of the electrochemical reaction in the least squares setting has been assumed.

Of (18) we have:

\[ c_{f_2} = -1.25e^{-5}C^{-2} \]

\[ d_{f_2} = 0.001C^{-1} \]

\[ e_{f_2} = 0.97 \]
Thermal model

The overvoltages $r$, $s$ and $t$ present in the electric model are a function of the temperature, it is for this reason that the thermal model is raised, in order to obtain the value of this one, for which a balance of energy is made in the electrolyser with (16).

$$\Delta E = E_{\text{entrada}} - E_{\text{salida}}$$ (16)

$$\Delta E = Q \cdot P \cdot \Delta V$$

Where:
- $\Delta E$: Energy shift
- $Q$: Heat at the entrance

Because the mathematical model focuses on the phase change of the solution (electrolyte dissolved in water) that occurs by means of an electrochemical reaction at atmospheric pressure, the work ($P\Delta V$) is neglected in (17).

$$\frac{dE}{dt} = Q$$ (17)

In order to calculate the behaviour of temperature over time, it is necessary to calculate all the heat involved in the energy balance and obtain the resulting heat, as expressed in (18) [11].

$$C_i \frac{dT}{dt} = \dot{Q}_{\text{generado}} + \dot{Q}_{\text{electrolito}} - \dot{Q}_{\text{perdido}}$$ (18)

Where:
- $C_i$: Thermal capacitance

Heat generated

The heat generated is the one contributed to the solution in the reaction due to the irreversibilities in the electrolysis process, by means of (19) this energy transfer is modelled.

$$\dot{Q}_{\text{generado}} = W_{\text{eléctrico}} (1 - n_U)$$ (19)

The voltage efficiency relates the thermoneutral voltage (reversible) and the actual voltage (irreversible) applied to the cell through (20).

$$n_U = \frac{U_{\text{rev}}}{U_{\text{irrev}}}$$ (20)

The voltage efficiency may be greater than the unit because the irreversible voltage is less than the reversible voltage.

Electrolyte heat

In the literature of alkaline cells (AFC) when modeling is considered, the energy provided by the electrolyte in the reaction is not studied. Contrary to the previous thing in this investigation the energetic contribution of the conductor of second species for this process is analyzed.

The heat of the electrolyte models the calorific or energy potential provided by KOH or NaHCO during the electrolysis of water, for its calculation the speed constant ($k$) and the concentration ($C_A$) must be taken into account by means of (21) [14].

$$\dot{Q}_{\text{electrolito}} = kC_A^2$$ (21)

The speed constant varies with temperature as described by (22) [15] [16].

$$k = k_0 e^{\frac{-E}{RT}}$$ (22)

Where:
- $E$: Activation energy
- $R$: Ideal gas constant ($8.3144 \frac{J}{mol^oC}$)

For the calculation of the frequency factor ($K_0$) the moles of the reagents, and of the products must be considered, as well as it expresses it.

$$k_0 = \frac{[H_2^2][O_2^0]}{[H_2O]}$$ (23)

It is necessary to know the activation energy ($E$) to determine the constant speed of the reaction, thus establishing an energy variation at standard conditions.
(T= 25 °C, and P°=1 bar), at how the electrochemical reaction is carried out experimentally (24).

$$\Delta E^\circ = \Delta H^\circ - (\Delta n)RT$$  \hspace{1cm} (24)

To determine the concentration (CA) it is necessary to identify the solubility of potassium hydroxide (119 g in 100 g of water), and sodium bicarbonate (10.3 g in 100 g of water), taking into account that 900 g of distilled water are used during the process.

**Heat lost**

The heat lost models the amount of energy expelled into the environment, by means of (25) the above is shown. This is the expression that finally allows the calculation of the temperature [17].

$$\dot{Q}_{perdido} = \frac{T_r - T_a}{R_t}$$  \hspace{1cm} (25)

Where:
- $T_r$: Reaction temperature
- $T_a$: Ambient temperature

The thermal resistance is calculated on the acrylic sheets that are part of the electrolyzer as expressed in (26).

$$R_t = \frac{L}{KA}$$  \hspace{1cm} (26)

Where:
- $L$: Thickness of acrylic sheet
- $K$: Thermal conductivity of acrylic
- $A$: Surface of acrylic sheet

With the above values of L, K and A, the thermal resistance of the acrylic film is calculated ($R_t = 6.66$ k/W), this value takes great relevance in the simulation.

**Implementation of the model in Matlab-Simulink®**

The thermodynamic variables (H, S, and G) used in the model have been obtained as a function of the standard conditions (T=25 °C, and P°=1 bar) of an electrochemical reaction, the commercial tool EES® was used.

For the implementation of the mathematical model in Simulink, the previously defined equations are added and the respective connection is made. Figure 5 shows the subsystems of the process, where you can see the proposed models that simulate the behavior of the electrolytic cell, in which the input variables are the voltage (13.8 V) supplied by the DC source in the process, and the electrolyte mass (in kg) in the solution, in order to analyze the reaction temperature and HHO volumetric flow.
To solve (11) because it is a nonlinear expression, the Newton-Raphson method was used that linearizes the function by an assumed tangent line obtained by applying a two-point rule.

**Results and analysis**

The modeling and simulation of the alkaline electrolyser takes into account the energy contributed by the electrolyte ($Q_{electrolyte}$) in the reaction, contrary to the approaches of the mathematical models of [11], [12], [17] consulted in the literature concerning this type of cells, in these investigations the calorific potential contributed by the second species conductor in the process is not considered. Next, the effect of the calorific potential of the electrolyte on the temperature, and flow (volumetric flow) of HHO when sodium bicarbonate ($\text{NaHCO}_3$) and potassium hydroxide ($\text{KOH}$) are used is analyzed.

Figure 6 shows the behaviour of the electrolyser temperature using, it was dosed every 5 g until reaching 20 g to perceive the increase in temperature at different concentrations of the electrolyte, the simulated maximum value is above 45°C. On the other hand, the establishment time for the different quantities supplied coincides in 25 s.

When comparing Figure 6 and Figure 7 it is important to highlight the difference between the temperatures, with 20 g of sodium bicarbonate is obtained in the simulation more than 25.8 °C, with the same amount of potassium hydroxide is above 45 °C the temperature of the reaction generated in the cell, this occurs because the solubility of KOH (119 g in 100 g of water) is higher compared to NaHCO$_3$ (10.3 g in 100 g of water), in turn the flow of the current increases, and the temperature rises; with this the directly proportional relationship between the variables is evident, before the increase of some of them the others are also increasing. The time of establishment of the temperature with KOH is less (25 s), that is to say, the reaction is faster due to the chemical properties of the electrolyte.

Figure 8 and Figure 9 show the variation of the HHO flow rate in the electrolyser with KOH, and NaHCO$_3$, according to the simulation a HHO flow rate above 0.02 L/s with potassium hydroxide (20 g) is recorded, in the case of sodium bicarbonate (20 g) a lower flow rate is produced (above 0.0006 L/s).

Figure 7 shows the variation of the electrolyser temperature using NaHCO$_3$, as well as with potassium hydroxide, the amount of sodium bicarbonate was simulated every 5 g to 20 g, a maximum temperature reached for this last concentration above 25.8 °C was recorded, and the settling time for all curves is 35 s.
The electric current circulating through the electrolyser affects the temperature as previously mentioned and the HHO flow of the cell, as the simulation increases the concentration of the electrolytes, the flow of the current increases, in the case of potassium hydroxide increases in greater proportion and for this reason produces 0.02 L/s of oxyhydrogen, when these values are compared with sodium bicarbonate (above 0.0006 L/s), KOH is established as the best electrolyte alternative for electrolytic cells.

Conclusions

The modeling was performed, and the simulation of an alkaline electrolytic cell that produces oxyhydrogen, in the thermal model the values of the thermal capacitance and thermal resistance influenced notably in the dynamic behavior of the temperature, because Ct adjusts its time of establishment and Rt can make vary its value.

The dynamic behavior in the simulation of the electrolyzer with potassium hydroxide was better in comparison of sodium bicarbonate, because in the flow (most significant variable) with KOH (20 g) is higher than 0.02 L/s, and with NaHCO₃ (20 g) is above 0.0006 L/s, allowing to confirm what is stated in the literature of alkaline cells, where it is established that the electrolyte with the most efficient operates is KOH.

The variables analyzed (temperature and flow) showed a behavior directly proportional to each other, ie, as the amount of electrolyte was increased (each 5 g to 20 g) both the temperature and flow increased, this behavior is presented because the current flow is gradually higher, thus happens experimentally in this type electrochemical processes.

In the simulation of the electric and chemical model, it was necessary to calculate some correcting coefficients of adjustment with the nominal operating conditions, and constructive parameters of the electrolyzer, the results were Alpha = 1.038, and Beta = 1.082, these values allow to establish the proximity or the existing closeness between the simulated mathematical model, and the behavior of an electrolytic cell experimentally.

References


